



# Ambiguity Fixing Results on an SDR Configured Notebook

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# Agenda

- Sogei GNSS SDR Objectives and Requirements
- Sogei GNSS SDR Architecture
- Pseudorange and Carrier Phase measurements
- RTK Processing
- Ambiguity Fixing Results
- Conclusions and Remarks

## The Mission



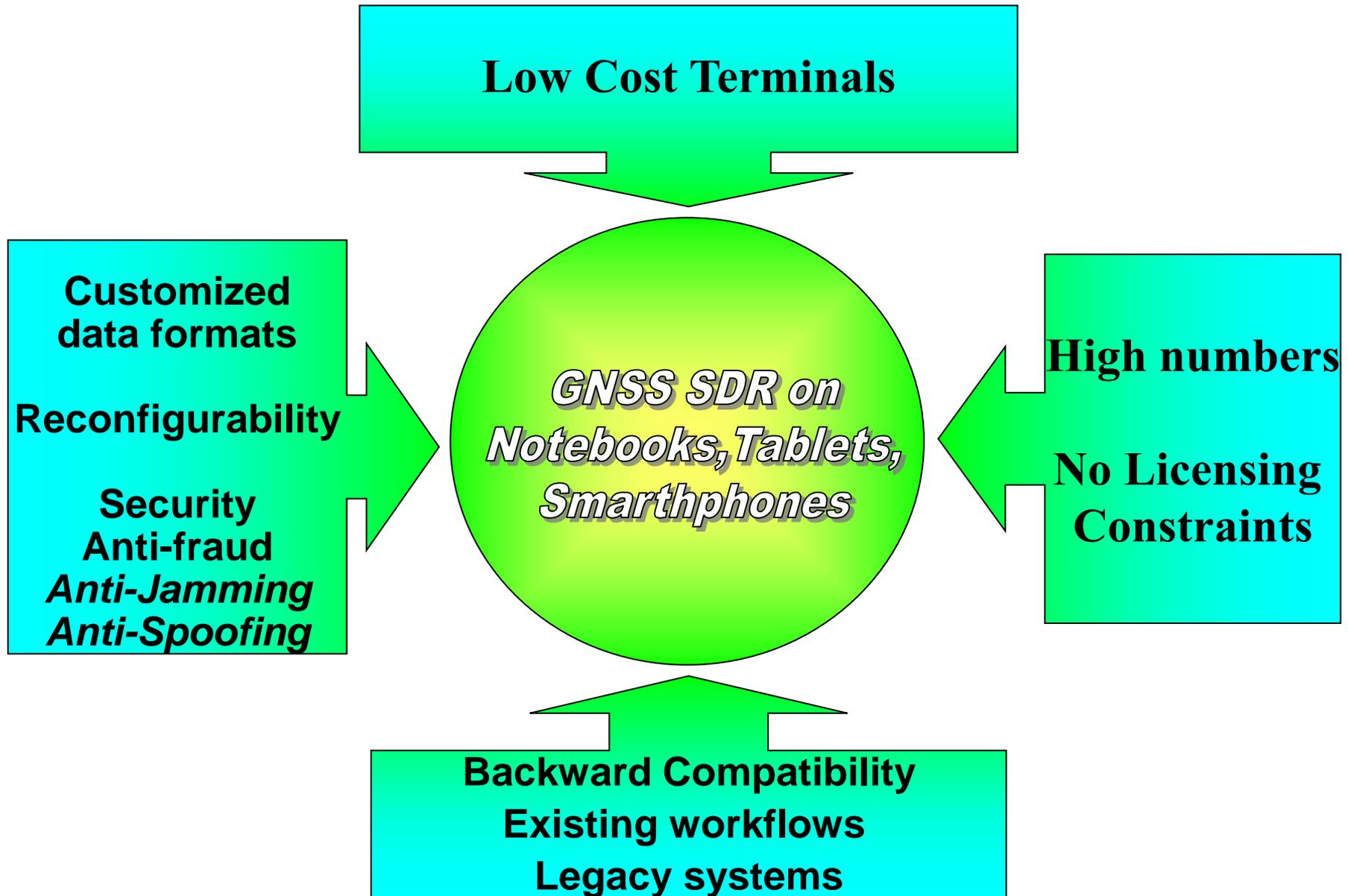
In 2003 Sogei's unique shareholder (the Italian Ministry of Economy and Finance) committed Sogei to follow the development of **GNSS Advances**

Sogei's R&D team began working in advanced GNSS technology for Institutional Applications developments

Since 2004, Sogei is member of the Galileo Services Association



# Institutional Applications – General Requirements



# Institutional High Precision Surveying - GNSS Cadastral Surveying

Shadowed points:  
GNSS and Topographical  
instruments hybridisation

**Rilievo GPS : Punto Iniziale di Baseline (riga 1)**

Vertice iniziale di vettore GPS  
Identificativo Stazione: 100  
Unita' Di Misura : metri

Coord. X Geocentrica: 4636425.349  
Coord. Y Geocentrica: 1030598.281  
Coord. Z Geocentrica: 4243042.599  
Altezza Centro Antenna: 2.153

Inizio osservazioni  
Data: 08/04/2008 Ora: 9.47.00

Fine osservazioni  
Data: 08/04/2008 Ora: 9.47.00

Metodologia del rilievo  
 Baseline  RTK

Tipo ricevitore  
 Monofrequenza  Doppia frequenza

Valori DOP  
 GDOP  PDOP 3

Nota

Accetta Annulla Guida

**Rilievo GPS : Punto Finale di Baseline (Riga 2)**

SELEZIONE TIPO MISURA

Punto Finale di Vettore GPS  
Identificativo Punto: 600

Componente Dx: -98.038  
Componente Dy: -45.508  
Componente Dz: 117.384  
Altezza Centro Antenna: 0.00

Valori DOP  
 GDOP  PDOP 3

Matrice di Varianza-Covarianza

	X	Y	Z
X	0.0009	0.0001	0.0003
Y		0.0012	0.0002
Z			0.0015

RMS

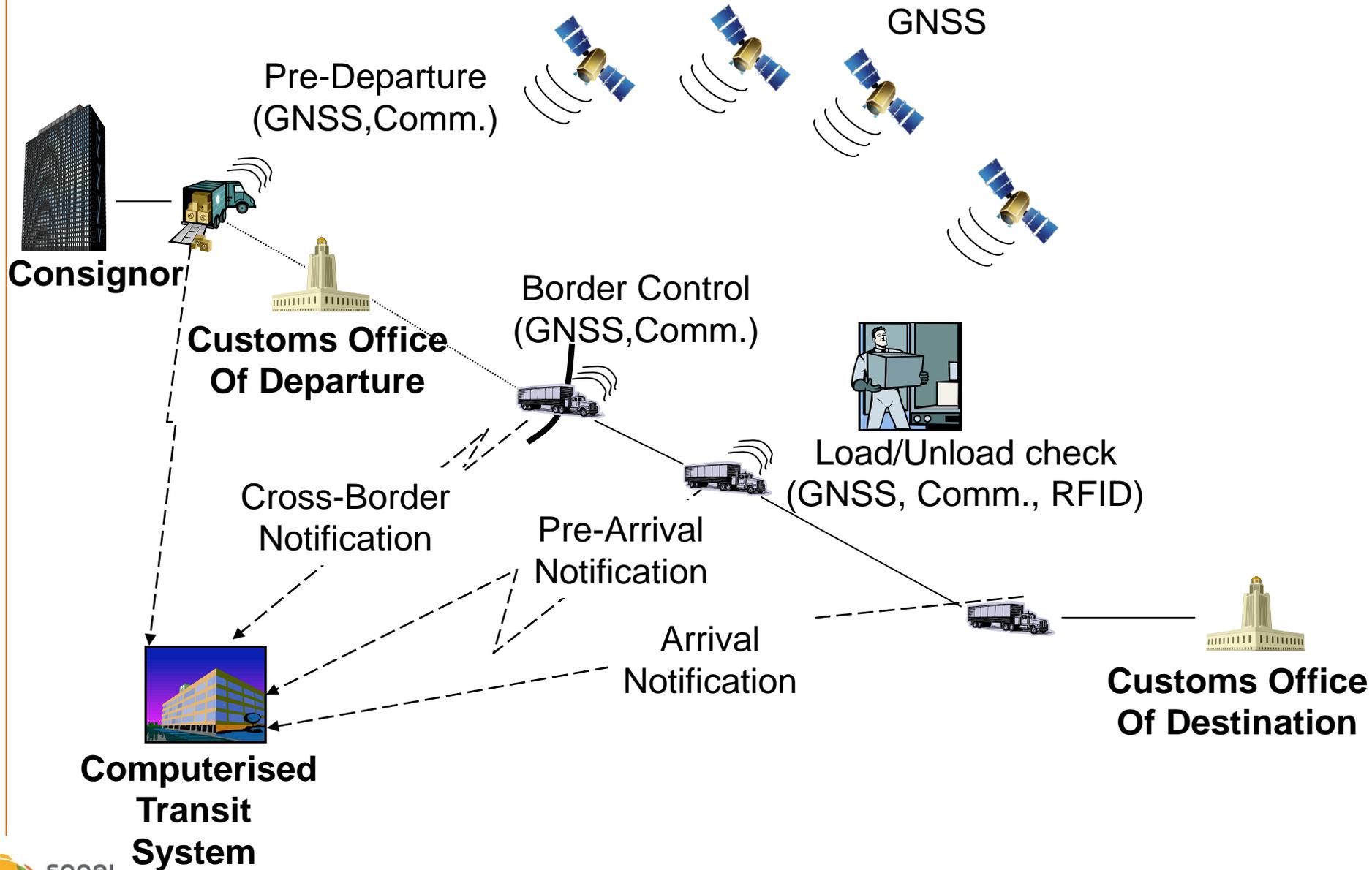
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Accetta Annulla Guida

PF01/136C/M1AAC

**Institutional Cadastral Surveying Software (PREGEO)**

# Customs Tracing and Tracking



## Sogei GNSS R&D pillars

- GRDNet (GNSS R&D Network) Solution-Independent **GNSS High Precision Augmentation**
- High Precision Software Receivers with **A/J** and **A/S**: **Sogei GNSS SDR**
- **Ubiquitous Outdoor/Indoor positioning**





# Sogei GNSS SDR progresses

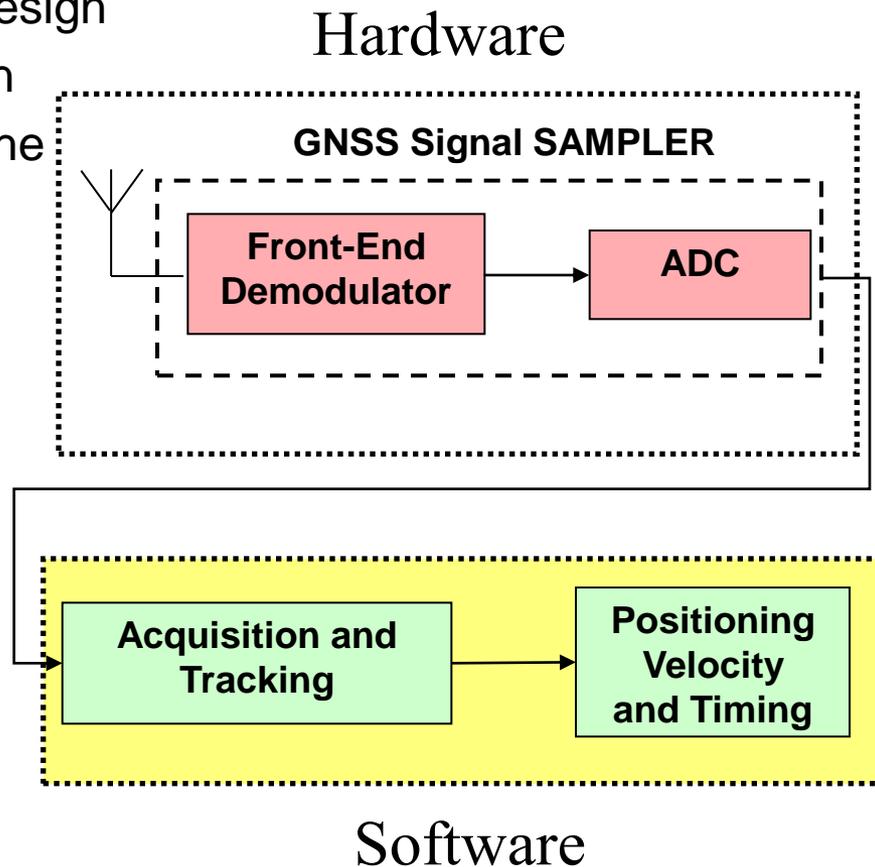
## Software Receiver on General Purpose Technology

Roberto Capua

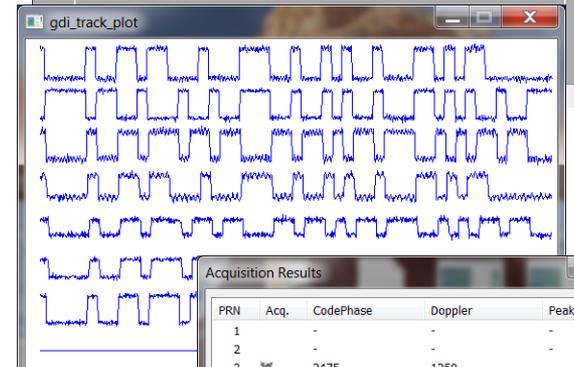
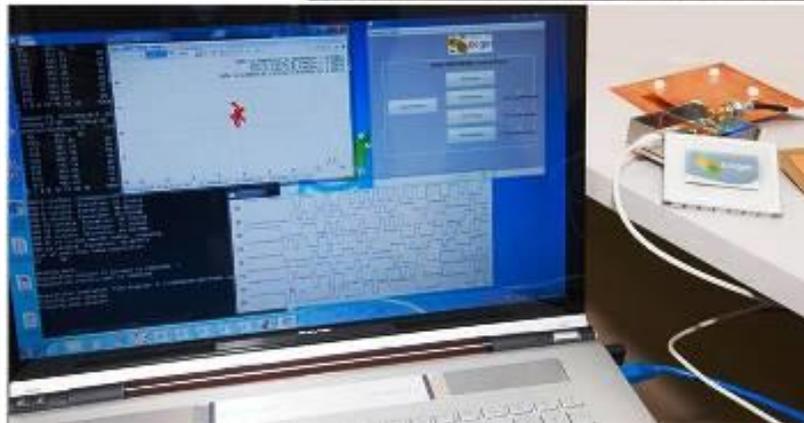
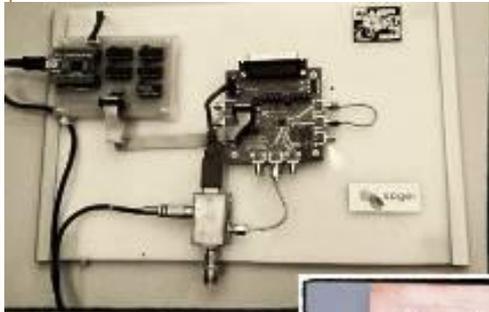
26 September 2014

## The SOGEI GNSS SDR Platform

- Objective: *Developing a low cost, flexible and free of license GNSS receiver for governmental applications running on **General Purpose Processors***
- L1/E1, WAAS/EGNOS, Code
- COTS Antennas and GNSS Front-End design
- TCP/IP Sockets Modules Communication
- Code/Carrier Look-Up Tables within Cache
- Development Language and tools:
  - ▶ C/C++
  - ▶ SIMD instructions
  - ▶ Parallel Programming
- **Fully Real-Time on a Notebook**
- **No FPGA/DSP**



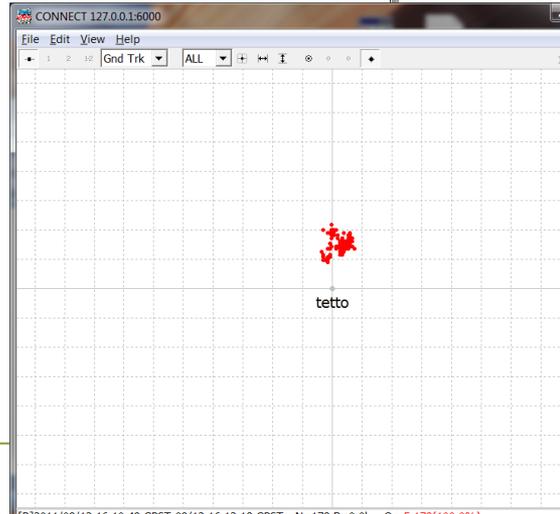
# GNSS Front-End and GUIs



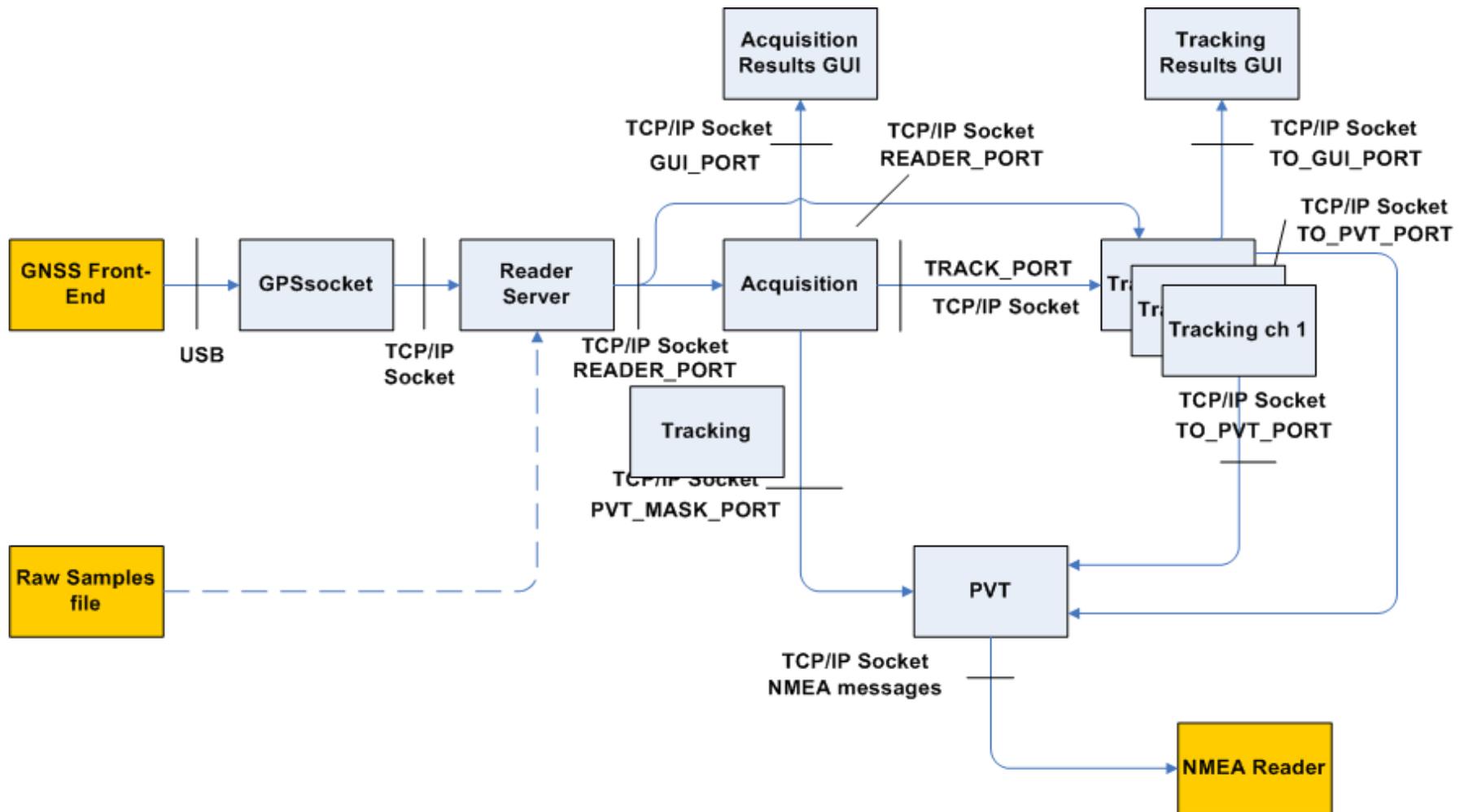
Acquisition Results

PRN	Acq.	CodePhase	Doppler	Peak
1	-	-	-	-
2	-	-	-	-
3	✖	2475	1250	-
4	-	-	-	-
5	-	-	-	-
6	✖	3702	400	-
7	-	-	-	-
8	-	-	-	-
9	-	-	-	-
10	-	-	-	-
11	-	-	-	-
12	-	-	-	-
13	-	-	-	-
14	-	-	-	-
15	-	-	-	-
16	✖	2734	-1200	-
17	-	-	-	-
18	✖	2791	-900	-
19	✖	2762	2450	-
20	-	-	-	-
21	✖	537	-2300	-
22	✖	361	1700	-
23	-	-	-	-
24	-	-	-	-
25	-	-	-	-
26	-	-	-	-
27	-	-	-	-
28	-	-	-	-

Packet 120001



# GNSS SDR Architecture



# Tracking Module

- GPS/SBAS channels
- *32-bits word input samples parallelization*
- Early-Minus-Late Correlation
- Multiplications by XOR and pre-computed logical operations
- Loops Filters specifications:

	Filter	Discriminator
<b>DLL</b>	2 <sup>nd</sup> order DLL	$D_{code} = \frac{I_{EL}I_P + Q_{EL}Q_P}{2(I_P^2 + Q_P^2)}$
<b>PLL</b>	2 <sup>nd</sup> order PLL (3 <sup>rd</sup> order selectable)	Atan(Q/I)
<b>FLL</b>	1 <sup>st</sup> order FLL (Switch-On/Switch-Off)	Atan2(cross,dot)/(2πT)

# SDR implementation of a Loop Filter

$$F(z) = C_1 + \frac{C_2}{1 - z^{-1}} = \frac{(C_1 + C_2) - C_1 z^{-1}}{1 - z^{-1}}$$

$$N(z) = \frac{k_0 z^{-1}}{1 - z^{-1}}$$

## C++ Filter implementation

```
PLL_OMEGA0 = (double)((8*parameters.pllNoiseBw*parameters.pllDamp)/(4*pow(parameters.pllDamp, 2)+1));  
PLL_TAU1 = (double)((parameters.pllK0*parameters.pllKd)/pow(PLL_OMEGA0, 2));  
PLL_TAU2 = (double)((2*parameters.pllDamp)/PLL_OMEGA0);
```

```
PLL_COST1 = (double)(PLL_TAU2/PLL_TAU1);  
PLL_COST2 = (double)(parameters.integrationTime/PLL_TAU1);  
FLL_COST1 = (double)(4*parameters.fllNoiseBw*parameters.integrationTime);
```

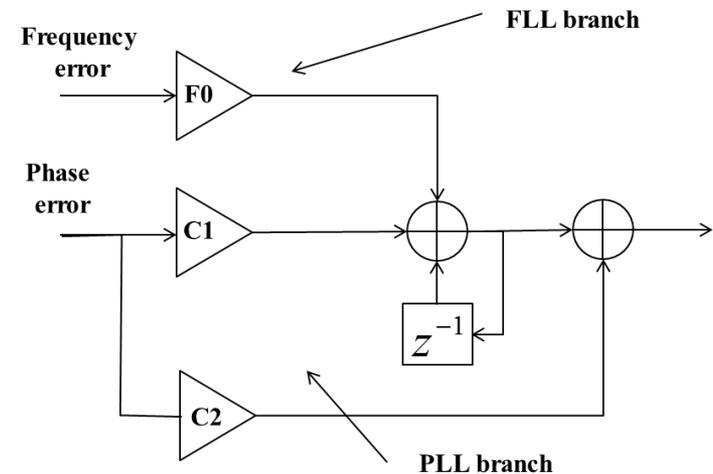
```
p11 = outPLL;  
f11 = outFLL;
```

```
yo1 = p11 * PLL_COST2;  
yo2 = p11 * PLL_COST1;  
yo3 = f11 * FLL_COST1;
```

```
yo4 = yo1 + yo3 + carrierLoopDelay1[channel];
```

```
output = (double)(yo4 + yo2);
```

```
carrierLoopDelay1[channel] = yo4;
```



# PVT Module

- Unscented Kalman Filter State vector:

Clock  
offset    Clock  
drift

$$x = \left[ x \quad y \quad z \quad | \quad \dot{x} \quad \dot{y} \quad \dot{z} \quad | \quad \overset{\swarrow}{b} \quad \overset{\swarrow}{\dot{b}} \right]^T$$

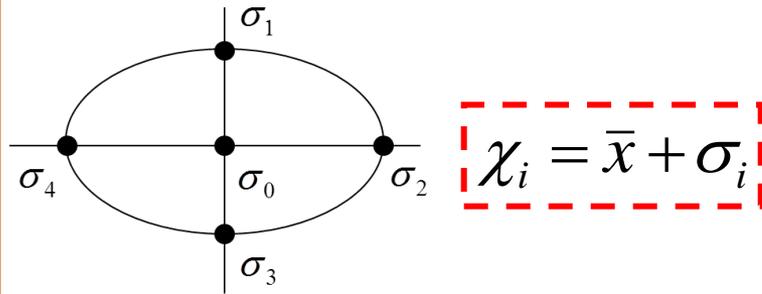
$$y = g(x) = \begin{bmatrix} PR \\ D \end{bmatrix} \begin{array}{l} \text{Pseudorange} \\ \text{Doppler} \end{array}$$

- Carrier Phase measurements through Integrated Doppler
- UKF (Unscented Kalman Filtering) processing:
  - ▶ **No linearisation and Jacobian calculation** needed
  - ▶ **Covariance matrix propagation by points** (2n+1)
  - ▶ Relaxed initial conditions constraints (no Bancroft needed)
  - ▶ Kalman Update phase as in EKF

## Propagation by points: the centrality of the Covariance

“It is easier to approximate a Gaussian distribution, than a non-linear function“

- Assuming a Gaussian distribution with mean  $\bar{x}$  and Covariance  $\sigma$
- We approximate the continuous distribution by a set of  $2n+1$  points (Sigma-Points):



### Initialization

$$M = \sqrt{(n+k) \cdot P_0^-}$$

$$S = \begin{bmatrix} 0 & -M \\ -M & +M \end{bmatrix}$$

$\sigma_i = i^{\text{th}}$  column of  $S$

$$\chi_0(i) = \hat{x}_0^- + \sigma_i$$

### Prediction

State

$$w_m^0 = \frac{\bar{k}}{n + \bar{k}}$$

$$w_m^i = \frac{1}{2(n + \bar{k})}$$

$$\bar{k} = \alpha^2 \cdot (n + \tilde{k}) - n$$

$$\chi_{k+1}(i) = f(\chi_k(i), u(k))$$

$$\hat{x}_{k+1}^- = \sum_{i=0}^{2n} w_m^i \cdot \chi_k(i)$$

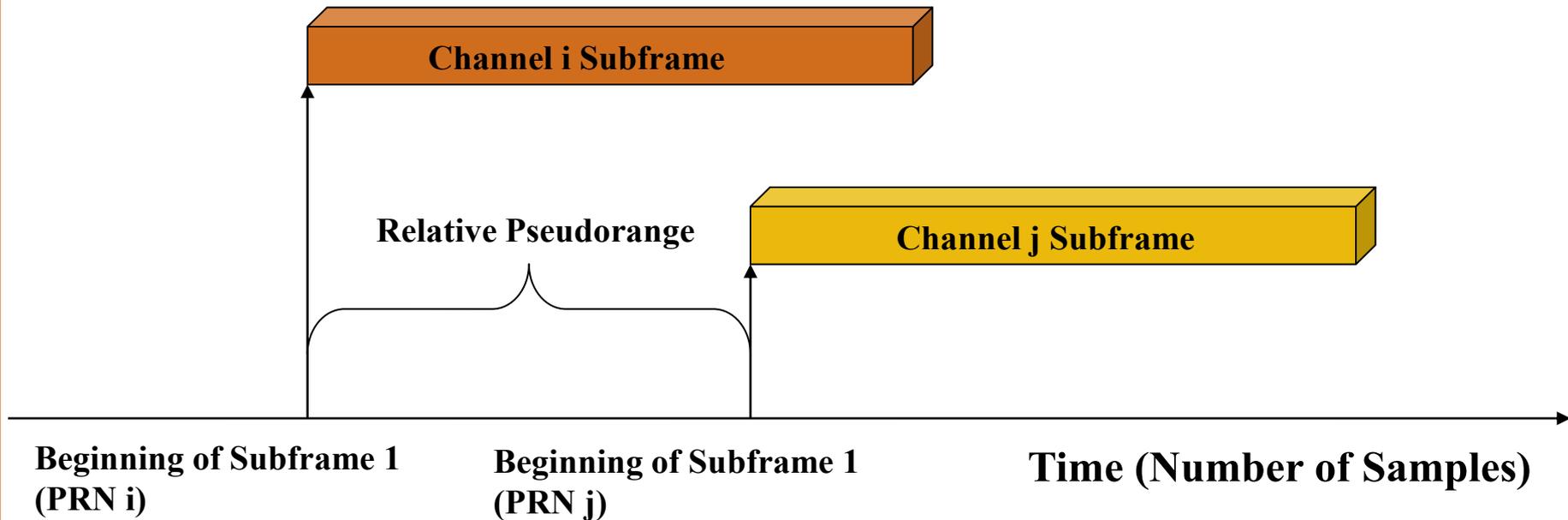
Measurements

$$Z_{k+1}(i) = h(\chi_k(i), u_k, t_k)$$

$$\hat{z}_{k+1}^- = \sum_{i=0}^{2n} w_m^i \cdot Z_k(i)$$

# The basic SDR Measurements challenge

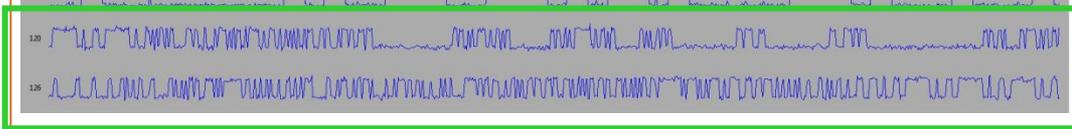
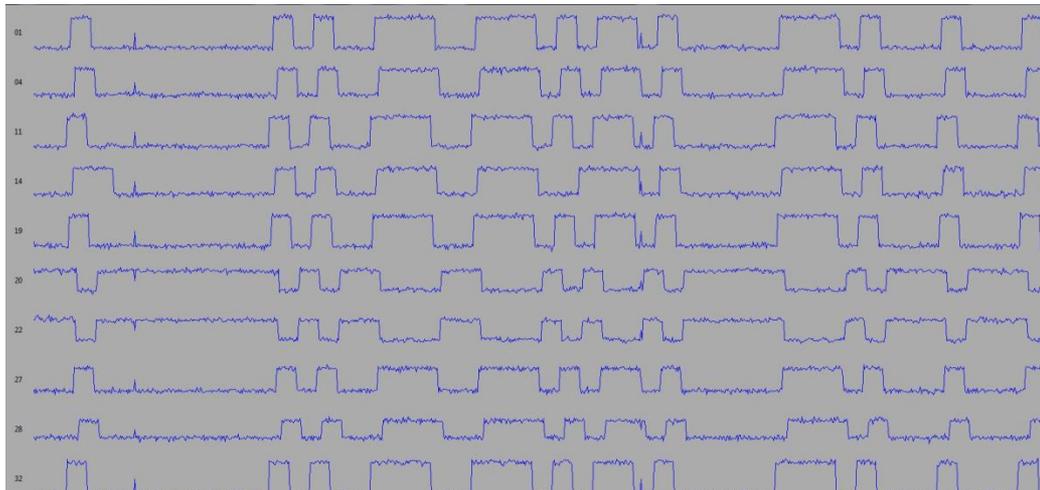
- In a Software Receiver sample data have **no absolute time reference**
  - The only timing is the progressing **number of samples count**
  - Messages are transmitted at the same time and received at different times due to different propagation times (satellite-user distances)
- ↓
- Pseudorange has to be calculated in a relative way from Subframe 1 starts (supposed to be transmitted at the same time by each satellite)



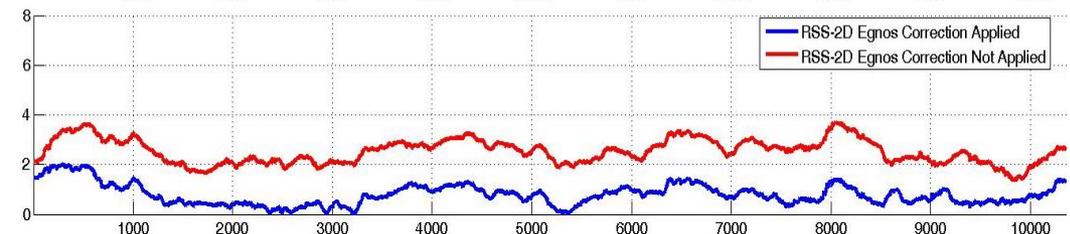
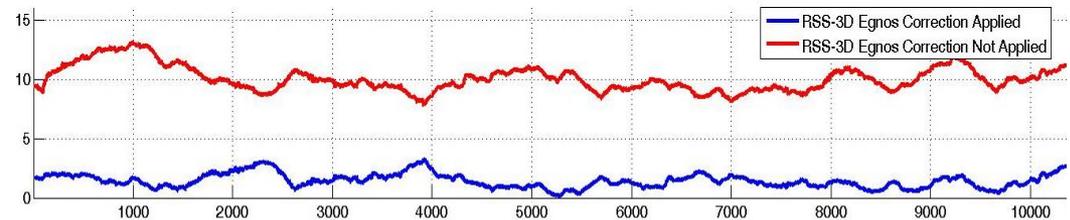
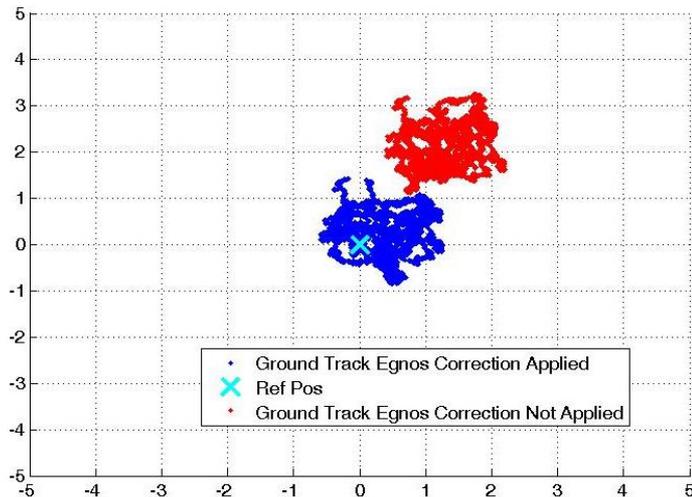
# PVT SDR implementation issues

- Data exchange:
  - ▶ Tracking results to be packed in blocks (e.g. 500 ms)
  - ▶ Check communication failure among components (e.g. Acquisition, Tracking, PVT)
- Pseudorange computation:
  - ▶ Avoid overflows of counters with proper resetting
- Real-Time constraints
  - ▶ Acquisition to be performed at a low rate (e.g. 30 s step) or after loss of lock

# EGNOS on the GNSS SDR



← SBAS Tracking Channels

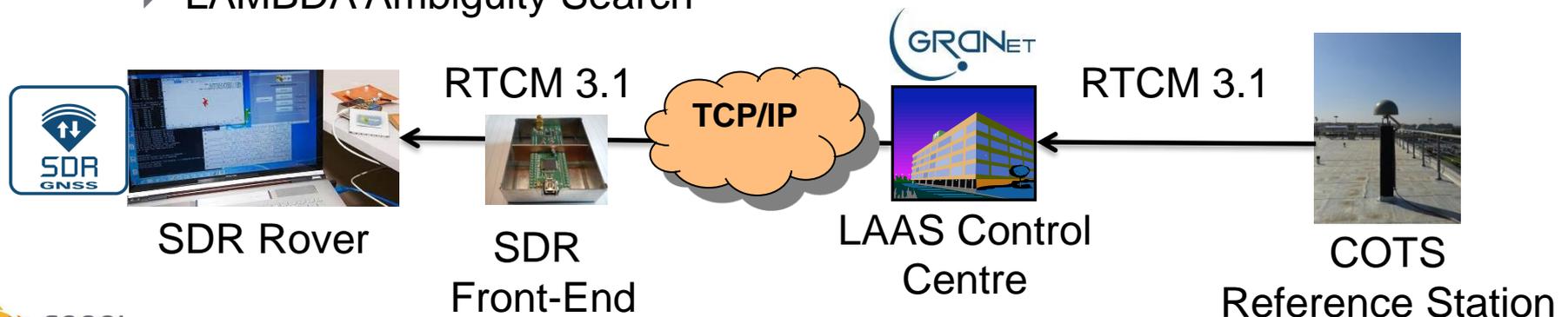


# GNSS SDR Criticalities and Constraints for RTK Processing

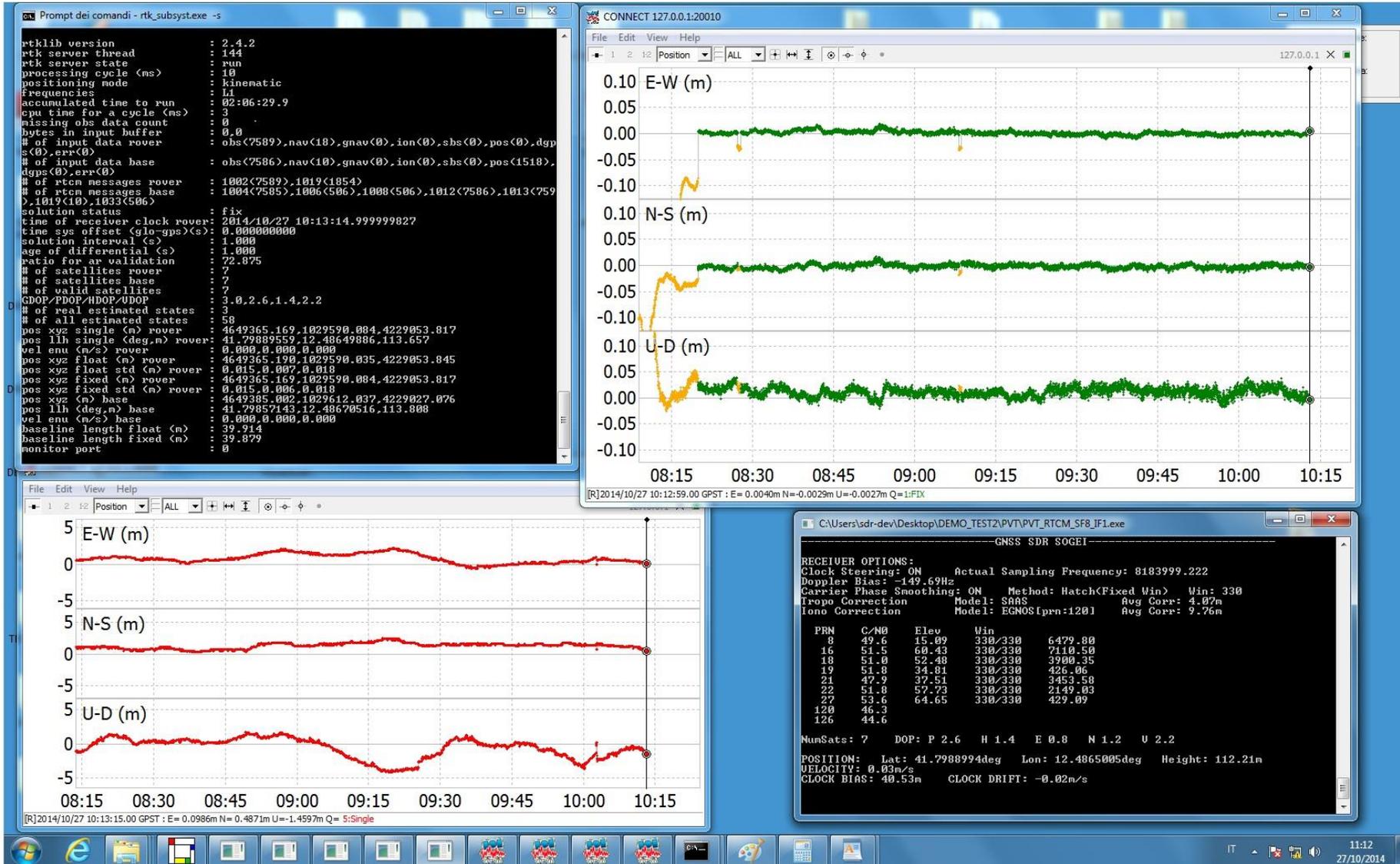
- **Computational Load:** GNSS SDR, fully working on a Notebook, provides measurements affected by quantization errors due to the maximum applicable sampling frequency
- **Receiver Clock error Compensation:** clock steering has to be applied in order to compensate receiver clock errors and generate the needed high quality phase measurements
- **Pseudorange Carrier Smoothing:** to be applied for reducing the impact of quantization errors
- **Initial Carrier Phase determination:** complex due to absence of time tagged measurements (only sequences of samples) and clock steering application
- **Mixed Hardware and SDR measurements for double differencing:** SDR Measurements Alignment and Synchronization wrt time tagged Reference Station ones
- **Measurements errors modelling:** as accurate as possible in order to limit feedbacks from clock steering (SBAS corrections, Tropo)

# RTK Processing and Test Case

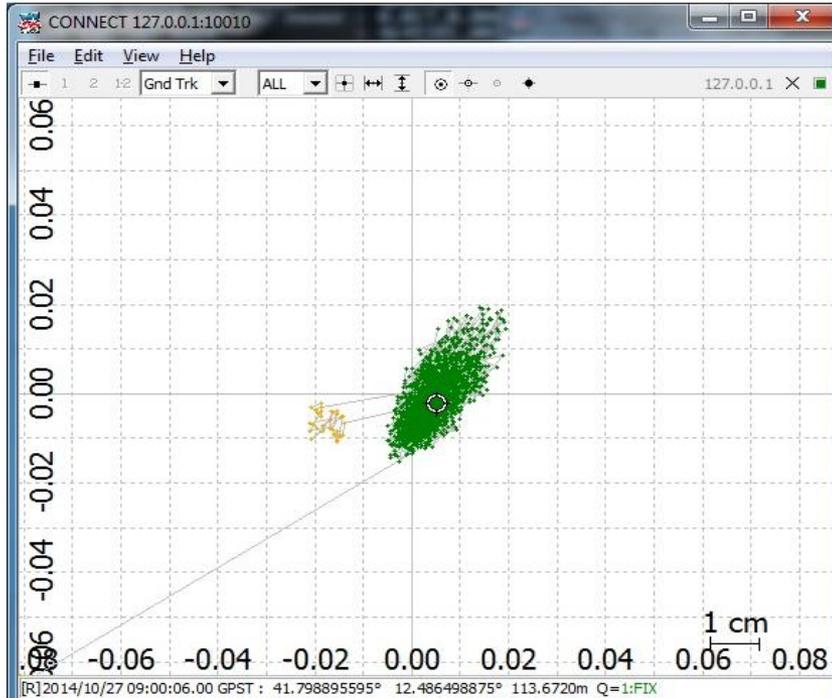
- Sampling frequency: 8.184 MHz
- Geodetic Reference Station data from a Local Augmentation Network
- GNSS SDR Rover with COTS surveying antenna
- Communication Interfaces toward the LAAS Service Centre:
  - ▶ Mobile Communication or internal LAN
  - ▶ NTRIP protocol
  - ▶ RTCM 3.1 1004 and 1006 messages
- RTK implementation:
  - ▶ Carrier-smoothed PR with SBAS corrections applied
  - ▶ Double Differences determination
  - ▶ LAMBDA Ambiguity Search



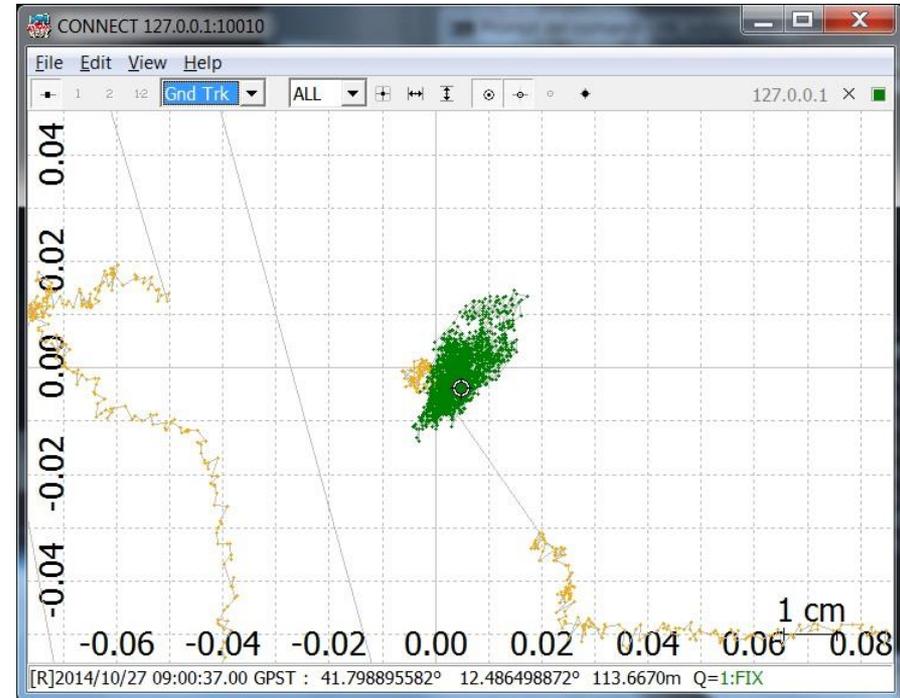
# SDR RTK Test Results



# SDR vs. Hardware Geodetic Receiver performances – Ground Track

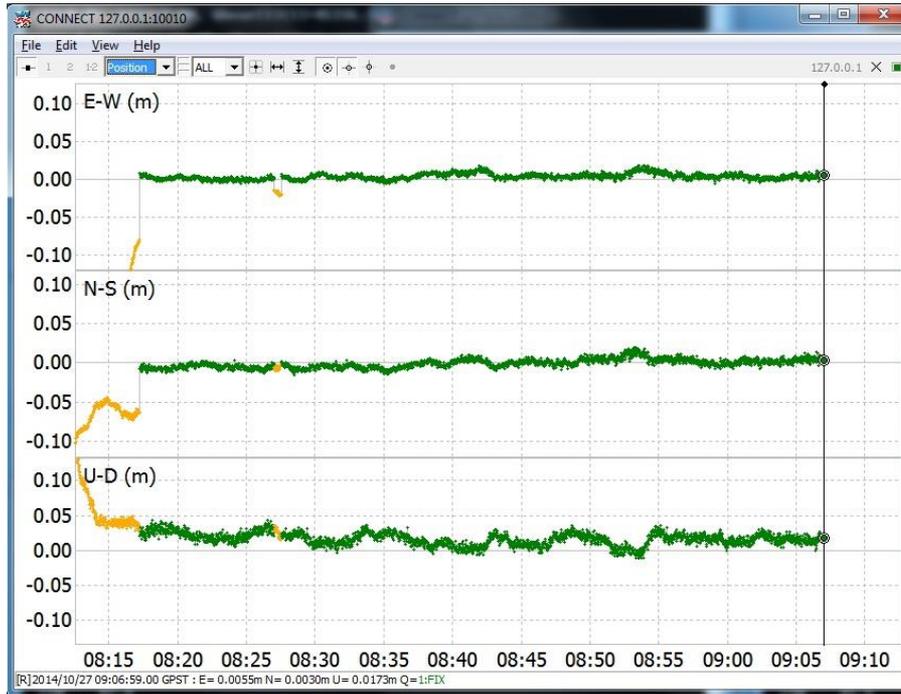


GNSS SDR Rover

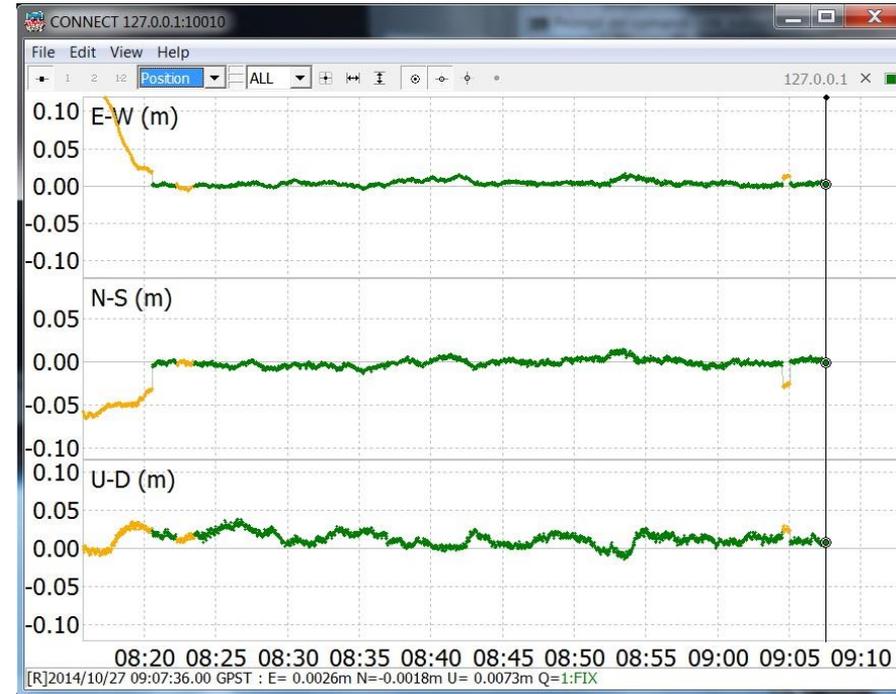


Commercial Hardware Rover

# SDR vs. Hardware Geodetic Receiver performances - ENU



GNSS SDR Rover



Commercial Hardware Rover

# Conclusions and Remarks

- Public Administrations need reconfigurable, reliable, low cost and open equipments
- Developed a GNSS SDR based, with internally designed Front-End, working in Real-Time on a Notebook without FPGA/DSP preprocessing/processing
- Pseudorange and Carrier Phase Measurements to be coherently dealt with
- RTK Test in a mixed environment:
  - ▶ GNSS SDR Rover
  - ▶ Geodetic Hardware Reference Station
  - ▶ Standard Interfaces: NTRIP/RTCM 3.1
- Test Results:
  - ▶ 3 cm 3D accuracy
  - ▶ Perfectly matching Commercial Geodetic receiver performances



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